3.1 INTRODUCTION

Pole-slip protection is commonly used in generator protection relays world wide. Some of the companies that developed pole-slip protection relays are listed below:

- ABB
- AREVA (ALSTOM)
- BASLER ELECTRIC
- BECKWITH ELECTRIC
- GENERAL ELECTRIC
- SEL
- SIEMENS

All pole-slip protection relays currently on the market use the impedance pole-slip protection method to determine when a generator could pole-slip. No relay can accurately predict when the generator is about to experience a damaging pole-slip. All the relays on the market will only trip the generator after it has pole-slipped once, which might be too late to prevent mechanical damage on the shaft.

3.2 DIFFERENCE BETWEEN “POLE SLIPPING” AND “OUT-OF-STEP” OPERATION

It is important to clarify the difference between “Pole Slipping” and “Out-of-Step” operation, since the term is generally used interchangeably in literature. In this thesis, “Pole slipping” is referred to as the occurrence when a synchronous machine rotor magnetic field slips with respect to the stator rotating magnetic field.

“Out-of-step” operation is referred to as the occurrence when a synchronous generator is out-of-synchronism with the rest of the network, but the generator rotor and stator magnetic fields may still be in synchronism with each other.
A generator can therefore fall “out-of-step” with the rest of the network without pole-slipping. A network with generators can become unstable without any generator pole-slipping. It must be emphasized that the terms “pole-slip” and “out-of-step” are often used interchangeably in textbooks and in the industry, while it is technically not the same.

The explanation for the above statements is illustrated in Figure 3.1 with a MATLAB setup consisting of two generators with ratings 1000 MVA and 5000 MVA respectively. Note that these are not practical generator sizes, but rather the sum of different smaller generators close to each other. The two generators are connected via step-up transformers to a transmission line. A bolted three-phase fault at bus B1 is applied for different durations to monitor stability and consequent pole slipping of the generators. The software of the MATLAB model are available on the CD attached in Appendix D.

Three scenarios were considered, namely:

- Applying a fault for a short duration so that the power system remains stable. The length of the transmission line is 200 km.

- Applying a long enough fault on the power system to cause the power system to become unstable. The length of the transmission line is 200 km.

- Applying a long enough fault on the power system to cause the power system to become unstable. The length of the transmission line is 20 km.

Figure 3.2 shows the speed, active power, transfer angle and internal power angles of the two generators. It can be seen that during the fault of duration 0.2 s, the speed of the 1000 MVA generator increases rapidly. The active power measured at bus B1 becomes zero, the transfer angle (mechanical rotor angle difference) between the two generators increases to 85° during the fault and the internal power angle of
the 1000 MVA generator becomes as high as 60°. After the fault all the quantities return to normal and the power system remains stable.

Figure 3.3 shows the speed, active power, transfer angle and internal power angles of the two generators with a 20 km transmission line. It can be seen that during the fault of duration 0.8 s, the speed of the both generators increases. The active power measured at bus B1 becomes zero and the transfer angle between the two generators increases rapidly during the fault. The internal power angle of the 1000 MVA generator becomes zero during the fault after the initial transient occurrence. The reason why the power angle is close to zero during the fault, can be explained by the following equation:

$$ P = \frac{V_1 \cdot V_2 \sin \delta}{X_{12}} $$  \hspace{1cm} (3.1)

where $P$ is the active power transfer

$V_1$ and $V_2$ are the voltages at bus 1 and bus 2 in a network

$X_{12}$ is the reactance between bus 1 and bus 2 in the network

$\delta$ is the transfer angle between bus 1 and bus 2

When the active power is zero, it means that the transfer angle $\delta$ will also be zero. However, when the fault is cleared, the active electrical power on the 1000 MVA generator returns and since the generator has sped up during the fault, the generator EMF is now out-of-synchronism with the terminal voltage. This condition causes the generator to pole-slip once the fault is cleared. It can be seen that the internal power angle (delta 1) oscillates between 180° and -180° rapidly, which indicates pole slipping. The 5000 MVA generator is not pole-slipping.

Figure 3.4 shows the speed, active power, transfer angle and internal power angles of the two generators with a 200 km transmission line. It can be seen that during the 0.8 s fault, the speed of both the generators increases. The active power measured at bus B1 becomes zero and the transfer angle between the two generators increases rapidly during the fault. After the fault is cleared, the internal power angle of both generators oscillate, but none of the power angles reach 180°, which means that the generators are not pole slipping. It can therefore be stated that, although the power system is unstable, the generators are not pole slipping due to the relatively high impedance of the transmission line connecting them.
Figure 3.2: Graphs of generator speed, active power, transfer angle and internal power angles against time (s) for a stable power system (200 km line)

Figure 3.3: Graphs of generator speed, active power, transfer angle and internal power angles against time (s) for an unstable power system with a generator pole slipping (20 km line)
Power swings occur when the power transfer angle of two generation units in a network oscillates with respect to each other. A generation unit can be defined as a group of generators, which are relatively close to each other. Considering the situation in South Africa, the Eskom network can be approximated by two generation units. The power stations located in the Mpumalanga province can be represented by one generation unit, while the Koeberg Nuclear Power Station in Cape Town can be represented by the other generation unit. These two generation units are interconnected with a long transmission line (longer than 1000 km). Since the impedance of the transmission line between the two generation units is high, the power system is susceptible to severe power swings.

The most common cause of power swings is faults that occur on the network. Switching of large loads can also cause power swings. Figure 3.5 shows a simplified power system with two generators. If a fault remains on the system for too long, the power transfer angles of the two generation units can differ by more than 180°. If the power transfer angle difference between two generators is 180°, one of the generators (the smallest one) could pole-slip.

During power swings, the voltage in the network will also vary. When Figure 3.5 is considered, the physical RMS voltage will be zero on the transmission lines (somewhere between buses C and D) when the

---

**Figure 3.4:** Graphs of generator speed, active power, transfer angle and internal power angles against time (s) for an unstable power system without any generator pole slipping (200 km line)

### 3.3 Power Swings

Power swings occur when the power transfer angle of two generation units in a network oscillates with respect to each other. A generation unit can be defined as a group of generators, which are relatively close to each other. Considering the situation in South Africa, the Eskom network can be approximated by two generation units. The power stations located in the Mpumalanga province can be represented by one generation unit, while the Koeberg Nuclear Power Station in Cape Town can be represented by the other generation unit. These two generation units are interconnected with a long transmission line (longer than 1000 km). Since the impedance of the transmission line between the two generation units is high, the power system is susceptible to severe power swings.

The most common cause of power swings is faults that occur on the network. Switching of large loads can also cause power swings. Figure 3.5 shows a simplified power system with two generators. If a fault remains on the system for too long, the power transfer angles of the two generation units can differ by more than 180°. If the power transfer angle difference between two generators is 180°, one of the generators (the smallest one) could pole-slip.

During power swings, the voltage in the network will also vary. When Figure 3.5 is considered, the physical RMS voltage will be zero on the transmission lines (somewhere between buses C and D) when the
The power transfer angle difference between the two generator EMFs is $180^\circ$. The point in the network where the voltage becomes zero is referred to as the electrical centre.

![Figure 3.5: Simplified power system consisting of two generation units](image)

### 3.4 Impedance Scheme Pole-Slip Protection

The impedance type pole-slip protection function works on the principle that the relay calculates the impedance (by measuring voltage and current) at a specific point in the network from which the relay can estimate what the power angle difference between the two generators are. This section gives an in-depth theoretical explanation of how impedance pole-slip protection relays typically work.

With the relay located at bus A in Figure 3.5, the impedance that the relay will see is determined as follows:

The total system impedance ($\tilde{Z}_{\text{Total}}$) is given as:

$$\tilde{Z}_{\text{Total}} = \tilde{Z}_{\text{genA}} + \tilde{Z}_{T1} + \tilde{Z}_{L} + \tilde{Z}_{T2} + \tilde{Z}_{\text{genB}}$$  \hspace{1cm} (3.2)

where $\tilde{Z}_{\text{genA}}$ is the internal steady-state complex impedance of generator A

$\tilde{Z}_{\text{genB}}$ is the internal steady-state complex impedance of generator B

$\tilde{Z}_{T1}$ is the complex impedance of transformer $T_1$

$\tilde{Z}_{T2}$ is the complex impedance of transformer $T_2$

$\tilde{Z}_{L}$ is the complex impedance of the transmission line

The current ($\tilde{I}$) that flows between the two generators is:

$$\tilde{I} = \frac{\tilde{E}_{\text{genA}} \angle \delta - \tilde{E}_{\text{genB}} \angle 0^\circ}{\tilde{Z}_{\text{Total}}}$$  \hspace{1cm} (3.3)

where $\tilde{E}_{\text{genA}}$ is the EMF of generator A with internal power angle $\delta$

$\tilde{E}_{\text{genB}}$ is the EMF of generator B with internal power angle $0^\circ$
The voltage \( \overline{V}_A \) on bus A (terminal voltage of generator A) is:

\[
\overline{V}_A = \overline{E}_{genA} - \overline{I} \cdot \overline{Z}_{genA}
\]

(3.4)

The impedance \( \overline{Z}_A \) that the relay at bus A will “see” is determined as follows:

\[
\overline{Z}_A = \frac{\overline{V}_A}{\overline{I}} = \frac{\overline{E}_{genA} - \overline{I} \cdot \overline{Z}_{genA}}{\overline{I}}
\]

\[
\therefore \overline{Z}_A = -\overline{Z}_{genA} + \frac{\overline{E}_{genA}}{\overline{I}}
\]

(3.5)

Substitution of equation (3.3) into equation (3.5) gives:

\[
\overline{Z}_A = -\overline{Z}_{genA} + \overline{Z}_{Total} \cdot \frac{|\overline{E}_{genA}| \angle \delta}{|\overline{E}_{genA}| \angle \delta - |\overline{E}_{genA}| \angle 0^\circ}
\]

(3.6)

The impedance \( Z_A \) can be plotted against the power angle difference between the two generators and against the voltage magnitudes \(|\overline{E}_{genA}|\) and \(|\overline{E}_{genB}|\). The internal power angle of generator B is chosen to be 0°. The power transfer angle difference (\(\delta - 0^\circ\)) between the two generators is therefore equal to \(\delta\). The “power transfer angle difference” will be referred to as the “transfer angle \(\delta'\)” throughout this thesis.

In order to simplify the illustration, it was chosen to use the per-unit system. This example makes use of 24 kV generators, 24 kV/400 kV step-up transformers and a 400 kV transmission line between the two transformers. The generator EMFs are chosen to be \(|\overline{E}_{genA}| = 24kV\) (or 1 pu) and \(|\overline{E}_{genB}| = 21.6kV\) (or 0.9 pu).

The impedances used in this illustration are as follows:

24 kV Generator A: \(R_a = 0.001\) pu and \(X_a = 0.3\) pu (\(\overline{Z}_{genA} = 0.001 + j0.3 \) pu)

24 kV Generator B: \(\overline{Z}_{genB} = 0.001 + j0.01\) pu (represents infinite bus)

400/24 kV Transformers: \(\overline{Z}_{T1} = \overline{Z}_{T2} = 0.001 + j0.1\) pu

400 kV Transmission line: \(\overline{Z}_{t} = 0.05 + j0.1\) pu
The above impedances were chosen arbitrarily to illustrate the theoretical principle of operation of the impedance pole-slip protection relays, but can be considered as typical power system impedances. $S_{\text{base}}$ is chosen as 100 MVA and $Z_{\text{base}} = \frac{V_{\text{base}}^2}{S_{\text{base}}}$ for each section of the power system with a different voltage base.

Figure 3.6 shows the absolute value of the impedance that the relay measures ($Z_A$) vs. transfer angle ($\delta$). It can be seen that $|Z_A|$ is the smallest at $\delta = 180^\circ$ and the largest when $\delta = 0^\circ$.

![Figure 3.6: $|Z_A|$ vs. transfer angle $\delta$](image)

Figure 3.7 shows the voltage at bus A ($V_A$) and the current ($I$) vs. the transfer angle $\delta$. It can be seen that the current is a minimum at $\delta = 0^\circ$ and maximum at $\delta = 180^\circ$.

The voltage at the electrical centre ($E_{\text{elec}}$) of the power system is determined as follows:

$$E_{\text{elec}} = E_{\text{genA}} - i \cdot (Z_{\text{genA}} + Z_{A@\delta=180^\circ})$$  \hspace{1cm} (3.7)

where $Z_{A@\delta=180^\circ}$ is the impedance that the relay at bus A measures when $\delta = 180^\circ$.

From equation (3.7), the current $i$ can that flows from Gen A in the direction of the electrical centre (when $\delta = 180^\circ$), can be calculated as follows:

$$i = \frac{E_{\text{genA}} - E_{\text{elec}}}{Z_{\text{genA}} + Z_{A@\delta=180^\circ}} = \frac{E_{\text{genA}} - 0}{Z_{\text{genA}} + Z_{A@\delta=180^\circ}}$$  \hspace{1cm} (3.8)
It is shown in Figure 3.8 that the current as calculated in equation (3.8) is equal to the current that would flow if a physical short circuit occurs at the electrical centre location.

Figure 3.7: Current $|I|$ and voltage $|E_a|$ (at relay location) vs. power angle $\delta$

Figure 3.8 shows the voltage at the electrical centre $|E_{elec}|$ and the current $|I|$ vs. the transfer angle $\delta$. It can be seen that the voltage at the electrical centre is a maximum at $\delta = 0^\circ$ and is zero at $\delta = 180^\circ$. The current has a maximum value at $\delta = 180^\circ$ and a minimum value at $\delta = 0^\circ$.

Figure 3.8: Current $|I|$ and voltage $|E_{elec}|$ (at electrical centre) vs. power angle $\delta$
Figure 3.9 shows the complex impedance locus of $Z_A$ vs. the power angle $\delta$. The total system impedance between generator A and generator B is indicated by the red line. The other system impedances are also indicated with the relay (located at bus A) at the origin of the plot. The intersection of the total system impedance $Z_{\text{total}}$ and the impedance locus $Z_A$ occurs when $\delta = 180^\circ$.

The reason why the impedance locus of $Z_A$ crosses the total system impedance at $\delta = 180^\circ$ can be explained mathematically by considering equation (3.6):

$$
Z_A = -Z_{\text{gen}A} + Z_{\text{total}} \left( \frac{E_{\text{gen}A} \angle \delta}{E_{\text{gen}B} \angle \delta - E_{\text{gen}B} \angle 0^\circ} \right) \tag{3.9}
$$

When $\delta = 180^\circ$, it can be seen that the term in brackets in the above equation will be a scalar magnitude. Equation (3.9) can be written as follows:

$$
Z_A = -Z_{\text{gen}A} + (K) \cdot Z_{\text{total}} \tag{3.10}
$$

where $K$ is a scalar magnitude.
The vector $\vec{Z}_{total}$ is not drawn from the origin, since the relay is located at the origin. From equation (3.10) it can be seen that $\vec{Z}_A$ is proportional to $\vec{Z}_{total}$ minus the impedance $\vec{Z}_{genA}$. $\vec{Z}_A$ as described by equation (3.10) is proportional to what defines the total impedance vector $\vec{Z}_{total}$ in Figure 3.9. The $\vec{Z}_A$ impedance locus will therefore fall on the impedance vector $\vec{Z}_{total}$ when $\delta = 180^\circ$.

The point on the $\vec{Z}_A$ impedance locus (in Figure 3.9), where $\delta = 90^\circ$, is connected with dotted lines to both ends of the $\vec{Z}_{total}$ vector. It can be seen from Figure 3.9 that the angle $\theta$ that the dotted lines make at the $\vec{Z}_A$ impedance locus is also $90^\circ$. The angle $\theta$ is therefore equal to the power transfer angle $\delta$. Impedance pole-slip relays use $\theta$ to initiate tripping after the generator has pole-slipped once. When $\theta = 180^\circ$, the $\vec{Z}_A$ impedance locus will intersect the vector $\vec{Z}_{total}$. Alternatively, $\delta$ will be $180^\circ$ when the $\vec{Z}_A$ impedance locus crosses the vector $\vec{Z}_{total}$.

![Figure 3.10: Impedance locus of a typical out-of-step protection function with blinders][22]

Figure 3.10 illustrates the concept when tripping is initiated with a typical impedance type pole-slip relay. The swing locus is indicated as a straight line that will enter a Mho circle from the right and pass through blinder B during a pole-slip scenario. The swing locus will continue through the X-axis, and will exit through blinder A for an unstable swing. When the swing locus exits blinder A or the supervising Mho circle, generator tripping is initiated. When this happens, the generator has lost synchronism and must be
separated from the system [22]. For a stable power swing, the impedance locus will enter blinder B and will exit via blinder B again. Tripping will be blocked for a stable power swing.

3.5 **Impedance Relay Principle of Operation**

This section explains the method of transfer angle calculation by the impedance scheme as described in section 3.4. The steady state transfer angle calculation will form part of the new pole-slip protection function as is explained in Chapter 4. Figure 3.11 shows a power system with resistance neglected.

The measured impedances \( Z_1 \) and \( Z_2 \) can be determined at both sides of the network reactance \( jX \) as shown in Figure 3.11. It can be shown that the vector sum of the calculated impedances \( Z_1 \) and \( Z_2 \) must add up to the network impedance \( jX \) between them.

![Figure 3.11: Impedance scheme transfer angle calculation](image)

Figure 3.12 shows the power vectors of the sending and receiving end and the reactive power loss \( (Q_{\text{line.loss}}) \) over the reactance \( jX \). It can be shown that the angle of the apparent power at a point is equal to the angle of the impedance measured at that point.

Figure 3.13 shows the calculated impedance vectors \( Z_1 \) and \( Z_2 \) together with the power system impedance \( jX \). The angle of \( Z_1 = \frac{V_1 \angle 0^\circ}{I \angle \phi} = Z_1 \angle (-\phi) \) is the power factor angle at \( V_1 \). The angle of \( Z_2 = \frac{V_2 \angle \delta}{I \angle \phi} = Z_1 \angle (\delta - \phi) \) is the power factor angle at \( V_2 \). It can be seen that the sum of the absolute values of these two angles are equal to the transfer angle \( \delta \).

Impedance relays uses the vector \( Z_1 \) to determine point A in Figure 3.13. It is not necessary to measure the vector \( Z_2 \), since it is simply the line connected between point A and the network reactance \( jX \).
relay can calculate the transfer angle $\delta$ by trigonometric mathematics. Section 4.7 provides a detailed example regarding the calculation of the impedance transfer angle.

Figure 3.12: Transfer angle Power Vectors –

Figure 3.13: Transfer angle Impedance Vectors
Figure 3.14 explains how the network transfer angle is determined by the impedance principle. The following impedances are drawn in the R-X complex impedance plane:

- Generator transient direct-axis reactance: $jX'_d$
- Step-up transformer reactance: $jX_{tx}$
- Network impedance (transmission lines up to the infinite bus): $Z_{line} = R_i + jX_i$
- Total system impedance (including generator and transformer): $Z_{total}$
- The impedance as measured by the impedance relay: $Z_{relay} = R_r + jX_r$
- Calculated Impedance angle $\phi$ (also the power factor angle)
- Transmission line power angle: $\delta_{line} = (\phi + \alpha)$
The impedance measured by the relay is calculated as follows:

\[ |Z| = \frac{|V_a|}{|I_a|} \]  

(3.11)

where \( V_a \) is the generator terminal voltage (line to neutral)

\( I_a \) is the generator line current

Also,

\[ Z_i = R_i + jX_i \]  

(3.12)

Therefore:

\[ R_i = |Z_i| \cos(\phi) \]

\[ X_i = |Z_i| \sin(\phi) \]  

(3.13)

where \( \phi \) is the power factor angle

The measured impedance angle \( \phi \) is also the power factor angle:

\[ \phi = \tan^{-1} \left( \frac{X_i}{R_i} \right) \]  

(3.14)

The angle \( \phi \) can be positive or negative depending on the signs of \( X_i \) and \( R_i \). The calculation of the transfer angle as shown in Figure 3.13 is only valid for scenarios where no shunt loads are present close to the generator. Section 3.6 describes the modifications required to include the effect of shunt loads in the transfer angle calculation algorithm.

### 3.6 The Effect of Shunt Loads on Impedance Relays

#### 3.6.1 Introduction

The pre-fault transfer angle between the generator EMF and the infinite bus as calculated by an impedance relay depends on the network impedance. The transfer angle over the transmission line will increase for each generator in parallel that generates active power than what an impedance relay would calculate without considering generators in parallel. On the other hand, the transfer angle over the transmission line will be smaller for every shunt load that consumes active power close to the generator terminals than what an impedance relay would calculate without considering shunt loads.

*Transmission line feeders* are referred to as feeders that connect the power station under consideration to other power stations via transmission lines. *Shunt load feeders* are referred to as feeders that feed loads like large factories or municipalities nearby the power station under consideration.
3.6.2 THEORETICAL ANALYSIS

Figure 3.15 shows a power system with four generators and three “infinite buses” and shunt loads. By definition, an infinite bus can be regarded as a section in the network where the voltage at that bus is behind a zero (or very small) impedance.

The pole-slip relay will use Infinite Bus 1 and 2 as the reference to determine the transfer angle of generators 1 and 2 respectively. The transfer angle is the angle between the generator EMF and the infinite bus.

The Loads 3 and 4 will not have a considerable influence on the transfer angle calculation if the paralleled impedance of transmission lines $T_{line3}$ and $T_{line4}$ is less than 5% of the paralleled impedance of $T_{line1}$ and $T_{line2}$. However, the shunt loads (Load 1 and 2 in Figure 3.15) will cause the transfer angle calculation to be inaccurate if the shunt loads are ignored in the transfer angle calculation. If the amount of active power supplied by Generator 2 is equal to the active power consumed by shunt loads 1 and 2, the transfer angle over the transmission lines will be calculated correctly by a conventional impedance relay.

From equation (3.11) in per-unit notation, the generator current is calculated as follows:

$$I_a = \frac{V_a}{Z_a}$$  \hspace{1cm} (3.15)

$$S_a = \frac{V_a \cdot V_a^*}{Z_a^*}$$  \hspace{1cm} (3.16)

$$= \frac{V_a^2 \angle 0}{Z_a^*}$$

$$\therefore Z_a = \frac{|V_a|^2}{S_a}$$  \hspace{1cm} (3.17)

where * denotes the complex conjugate

$S_a$ is the generator apparent power
The effect of the shunt loads 1 and 2 and Generator 2 in parallel with Generator 1 will cause equation (3.17) to be inaccurate. To compensate for the extra generator and shunt loads, $\bar{Z}_{a,\text{corrected}}$ is calculated as:

\[
\bar{Z}_{a,\text{corrected}} = \frac{V_{pu}^2}{\phi} = \frac{\left(\left(P_{\text{Trfr}1} + P_{\text{Trfr}2} - P_{\text{Shunt}}\right) + j\left(Q_{\text{Trfr}1} + Q_{\text{Trfr}2} - Q_{\text{Shunt}}\right)\right)}{V_{pu}^2}
\]

(3.18)

\[
\bar{Z}_{a,\text{corrected}} = \frac{\left|V_{pu}\right|}{P_{\text{Line_Total}} - jQ_{\text{Line_Total}}}
\]

Note that the transformer active and reactive powers are used instead of the generator power to include the effect of reactive power loss over the transformer.
From equation (3.18), the angle of $Z_{a\text{ corrected}}$ is calculated as:

$$
\phi_{\text{corrected}} = \tan^{-1} \left( \frac{Q_{\text{line total}}}{P_{\text{line total}}} \right)
$$

(3.19)

$$
|Z_{a\text{ corrected}}| = \frac{|V_{\text{pu}}|^2}{\sqrt{(P_{\text{line total}})^2 - (Q_{\text{line total}})^2}}
$$

(3.20)

From Figure 3.14, the angle $\alpha$ is calculated as:

$$
X_{a\text{ corrected}} = |Z_{a\text{ corrected}}| \cdot \sin(\phi_{\text{corrected}})
$$

(3.21)

$$
R_{a\text{ corrected}} = |Z_{a\text{ corrected}}| \cdot \cos(\phi_{\text{corrected}})
$$

(3.22)

$$
\alpha = \tan^{-1} \left( \frac{X_{\text{line}} - X_{a\text{ corrected}}}{R_{a\text{ corrected}} - R_{\text{line}}} \right)
$$

(3.23)

The power angle over the transmission line is calculated from Figure 3.14 as:

$$
\delta_{\text{line}} = \alpha + \phi_{\text{corrected}}
$$

(3.24)

Section 4.7.1 provides more information on transfer angle calculation (angle between generator EMF and infinite bus).

3.6.3 PROPOSED METHOD OF A PRACTICAL IMPLEMENTATION

Section 3.6.2 provided the theoretical analysis of the effect of shunt loads. A practical implementation is to measure the real- and reactive power of the transmission line feeders as shown in Figure 3.16.

It can be seen from Figure 3.16 that the active- and reactive powers are measured on the transmission line feeders only (no shunt load measurements are taken). A device (like a summation CT) can be installed to summate the currents of all the transmission line feeders.

To implement the scheme without modifying the hardware on a conventional pole-slip relay, the summation device can give a 0 to 5A signal to the relay. A 1 A signal implies a 1 pu active power with the generator apparent power as base. With this method, the current output of the summation device can be fed back to any relay CT input. The analogue current signal can be converted to an active power value in the relay logics.
Alternatively, a 4-20 mA signal or LAN / LON / Profibus communication can be used to transmit the transmission line current magnitudes to the pole-slip relays.

Figure 3.16: Power System Layout with shunt loads

3.7 Transmission Line Impedance

This section describes how transmission line impedances will be used in the new pole-slip protection function. Transmission line per-unit impedances as obtained from transmission line manufacturer’s data, can be processed to obtain a typical per-unit impedance range for transmission lines, which can be used to test the new pole-slip protection function.

For example, let the transmission line parameters be:

\[ S_{\text{base}} = 628 \text{MVA} \]
\[ V_{\text{base}} = 275 \text{kV} \]
\[ Z_{\text{base}} = \frac{V_{\text{base}}^2}{S_{\text{base}}} = \frac{(275 \text{kV})^2}{628 \text{MVA}} = 120.42 \Omega \]
For a “Twin-Bear”-transmission line, the 275 kV line impedance is (shunt admittance neglected) [56]:

\[ Z_{\text{line}(\Omega)} = 0.059 + j0.304 \ \Omega/km \]  

(3.26)

The maximum MVA rating of the “Twin Bear” transmission line used above is 628 MVA [56]. Typical transmission line tables indicate that when a Twin Bear transmission line is loaded at 628 MVA, the maximum length that Twin-Bear transmission line can be is 61 km [56]. If the transmission line is longer than 61 km at 628 MVA, stability across the line can be lost.

The per-unit impedance value of 61 km transmission line is:

\[ Z_{\text{line}(\text{p.u.})} = \frac{Z_{\text{line}(\Omega)}}{Z_{\text{base}}} = \frac{0.059 + j0.304}{120.42} \ \Omega/km \]
\[ = 4.899 \times 10^{-4} + j2.524 \times 10^{-3} \ \text{p.u./km} \]
\[ = 2.989 \times 10^{-2} + j1.540 \times 10^{-1} \ \text{p.u.} \]  

(3.27)

A generator step-up transformer has an impedance of typically 0.1 pu to 0.15 pu. The 61 km Twin-Bear transmission line reactance (as calculated above) is 0.154 pu. The generator transient reactance is typically \( X_d' = 0.3 \) pu. This means that the largest portion of the transfer angle will typically be across the generator/transformer combination. In other words, the electrical centre is likely to be in the generator / transformer combination.

If a transmission line longer than 61 km is needed at 628 MVA, two Twin-Bear transmission lines can be used in parallel. Alternatively, a larger transmission line conductor like Zebra or Twin-Zebra can be used. The generator sizes of Eskom (South Africa) are typically 600 MW each. In some power stations (like Koeberg nuclear power station) larger generators are used.

When larger generators are used, the MVA base will be chosen as the generator MVA rating, which means the transmission line per-unit impedance will become larger. Due to the higher MVA demand, a larger transmission line conductor must be used (or lines in parallel).

A “rule-of-thumb” ratio between generator impedance and maximum transmission line impedance can be obtained. Figure 3.17 shows the per-unit reactances of different transmission lines at the stability limit. In other words, the reactances are calculated on the transmission line rated MVA base and at the maximum transmission line length (km) at the rated MVA.

It can be noted from Figure 3.17 that the transmission line reactances are in the range 0.08 pu to 0.175 pu. “Wolf” and “Hare” transmission lines are typically not connected directly to power stations, due to the small MVA capacity of these lines. The other lines (“Bear” and “Zebra”) will typically be used to connect
directly to the HV side of the generator step-up transformers. The per-unit reactances of these lines are in the range 0.135 pu to 0.18 pu [56].

![Figure 3.17: Transmission Line Per-Unit Reactances at Stability Limit](image)

When the generator MVA rating is chosen as MVA base, the ratio of transmission line impedance to generator and step-up transformer impedance are typically as follows at the transmission line stability limit:

\[
2 \leq \frac{X_d + X_{tr}}{X_{line}} \leq 4
\]  

(3.28)

It is shown in chapter 5 that the new pole-slip algorithm is tested for various transmission line scenarios. The ratio in equation (3.28) is handy to use for the validation of the pole-slip function. It is important to note that the combined parallel impedance of the transmission lines which remains after one transmission line is lost due to a fault is applicable in (3.28). The generator and transformer impedances in (3.28) also imply the paralleled impedance of all the generator/step-up transformers combined. Equation (3.28) was used to check the impedance values of the tested networks as will be shown in Table 5.2 of section 5.4.

Figure 3.18 shows the X/R ratios of the different transmission lines as obtained from typical line data [56].
Apart from reactance and resistance, a transmission line is also modelled as having a shunt capacitance at the sending and receiving end. The shunt capacitance is typically represented by admittance (inverse of impedance) as follows:

\[
A = G + jB
\]  

(3.29)

where

- \(A\) is the shunt Admittance (Siemens or Mho)
- \(G\) is the shunt Conductance
- \(B\) is the shunt Susceptance \((B = \frac{1}{X_c} = \omega C)\)

The Susceptance is incorporated in the equivalent PI-model as shown in Figure 3.19.
The conductance \( G \) in equation (3.29) is often neglected, while the susceptance is obtained from manufacturer’s datasheets. The effect of the susceptance is that it will “supply” reactive power into the transmission line which will tend to increase the transmission line voltage at the receiving end. The effect of larger admittance and smaller resistance for larger transmission lines will tend to increase the stability of the line.

The pole-slip protection function only needs to determine the behaviour of transmission lines between the generator and the closest other power station. Transmission lines longer than 80 km are typically modelled by including the shunt admittance as shown in Figure 3.19 [5]. The stabilizing effect of the shunt admittance is already taken care of in the transfer angle calculation in equation (3.24), since the voltage and current measured at the sending end of the transmission line includes the compensation effect of the shunt admittance. There is no need to include additional shunt admittances in the pole-slip algorithm (similar to shunt loads). The effect of shunt admittance on the measured voltage and current at the transmission line sending-end will tend to decrease the transfer angle over the transmission line, which consequently increases the stability in the network.

3.8 SHORTCOMINGS OF CONVENTIONAL IMPEDANCE POLE-SLIP RELAYS

This section presents the shortcomings of conventional impedance pole-slip protection relays by using an example case study. It is emphasized that the discussion to follow does not implicate any specific relay manufacturer. It simply highlights the shortcomings that are common to all impedance type pole-slip relays.

The network impedance as seen from the generator terminals must be known in order to set the impedance pole-slip protection function. Figure 3.20 shows a generator configuration of a typical power station. When all six generators are in operation, generators G1, G2 and G3 will typically be paralleled at the high-voltage side of the step-up transformers, while G4, G5 and G6 are also paralleled to form a separate group.

Two scenarios can be studied, namely case 1 and case 2. For case 1, all the tie-breakers in Figure 3.20 that are labelled \( N/C \) (normally closed), are closed and the tie-breaker that is labelled \( N/O \) is open. For case 2, all the tie-breakers are open.

For case 1, generators G1, G2 and G3 are paralleled at the transformer high-voltage sides. The effective network impedance that each generator will see from its terminals is its own step-up transformer impedance plus the paralleled impedance of the other two step-up transformers and generators plus the network impedance in parallel.
The impedance as measured by the relay at the terminals of generator G1 with generators G2 and G3 in parallel with G1 is as follows:

$$Z_{\text{Case } 1} = Z_{T1} + \left( \frac{1}{Z_{T2} + Z_{G2}} + \frac{1}{Z_{T3} + Z_{G3}} + \frac{1}{Z_{\text{Network}}} \right)^{-1}$$  \hspace{1cm} (3.30)

For case 2, generators G2 and G3 are out of service, but generator G1 is in operation. The effective impedance as measured by the relay at the terminals of generator G1 is as follows:

$$Z_{\text{Case } 2} = Z_{T1} + Z_{\text{Network}}$$  \hspace{1cm} (3.31)

The network impedance ($Z_{\text{Network}}$) is typically much greater than the combined impedance of the generators with their step-up transformers. This means that the effective impedance for the paralleled generators ($Z_{\text{Case } 1}$) is considerably smaller than the impedance ($Z_{\text{Case } 2}$) where generator G1 is operating without other generators in parallel.

Figure 3.21 shows a screen snapshot of the user interface of a typical pole-slip relay. The impedance $Z_A$ is the impedance as calculated by equations (3.30) and (3.31). For the paralleled generators G1, G2 and G3, the impedance $Z_A$ is chosen to be 0.24 pu. $Z_B$ is the generator internal impedance and is chosen to be 0.34 pu in the reverse direction (or -0.34 pu). Although $Z_A$ and $Z_B$ are arbitrary values, these values can be regarded as typical values.
For this specific pole-slip relay manufacturer, $Z_C$ is calculated to be $0.8 \times Z_{Tx}$ and defines the border between Zone 1 and Zone 2 as is indicated in Figure 3.21 and Figure 3.22. The transformer impedance is chosen to be 0.1 pu, which means $Z_C = 0.8 \times 0.1 = 0.08$ pu. When the calculated impedance passes through Zone 1, it means the electrical centre is in the generator/transformer, and tripping should take place as soon as possible.

When the calculated impedance passes through Zone 2, the electrical centre lies in the network and tripping need not take place instantaneously. Some users prefer that pole-slip tripping is avoided when the electrical centre is in Zone 2 [1].

In this case study, the warning angle is set at 110°, while the tripping angle is set at 90°. The tripping angle is represented by the purple circle and the warning angle by the orange circle in Figure 3.21. The warning angle is measured by connecting $Z_A$ and $Z_B$ with straight lines to any common point on the orange warning circle. The angle that this triangle makes on the warning circle will be 110°. If the warning angle is
increased to say, $120^\circ$, the orange circle will get smaller to allow for the greater angle. The tripping angle works on a similar principle.

The impedance will typically be in the top-right quadrant of the R-X plane during normal operation. During a power swing, the impedance will approach the warning circle from the right. When the impedance enters the warning circle, the relay will give a pole-slip warning. When the impedance crosses the $Z_A - Z_B$ line, an out-of-step condition is detected. If the impedance swing continues to the left of the R-X plane and exits the trip-angle circle, the relay will issue a pole-slip trip, provided that the power swing frequency is between 0.2 Hz to 8 Hz. The trip angle is normally set at $90^\circ$ to minimize the current breaking stress on the generator circuit breaker.

If $Z_A$ in the relay is set for normal operation (case 1), and generators G2 and G3 are out of operation, the pole-slip function will not detect slips in Zone 2 that have an impedance greater than the preset $Z_A$ value. When generator G1 is operated alone (case 2), the network impedance $Z_A$ can be as great as 10 times the value that is preset to be $Z_A$. Figure 3.23 shows the impedance line for $Z_A = 2.4$ pu. The impedance locus can cross the $Z_A - Z_B$ line anywhere during power swings. With a $Z_A$ value set at 0.24 pu, the relay will not detect power swings (or out-of-step operation) if the impedance locus crosses the $Z_A - Z_B$ line at $0.25 \angle 80^\circ$, for example. At this impedance, the out-of-step condition can cause serious mechanical stress and damage on the generator without detecting the out-of-step condition.

By setting the relay at $Z_A = 2.4$ pu for case 2, the tripping and warning angles will not be accurate if the generators are operated in normal configuration (i.e. three generators in parallel). A tripping angle that is set at $90^\circ$, will issue a trip once the angle has reached approximately $20^\circ$. This could possibly cause the breaker to experience damage if it is only rated to break the current at an angle of $90^\circ$. A network impedance $Z_A$ can be chosen to be an average for the different switching scenarios, but the accuracy of the impedance pole-slip protection function cannot be guaranteed throughout different switching configurations.

When set up correctly, the impedance pole-slip scheme could eventually trip a machine that fell out-of-step, but it cannot trip a machine before it falls out-of-step. It is important to note that if the tie-breaker status changes to an configuration that is not normal, the impedance pole-slip protection relay will not work accurately anymore.
Chapter 3 discussed the method of operation of conventional impedance pole-slip relays. The algorithm used in the conventional impedance pole-slip relays was derived from first principles to get a proper understanding of the impedance scheme.

An example case study was investigated to determine how a conventional pole-slip relay will perform in certain network switching configurations. It was found that impedance relays can become inaccurate by switching in/out paralleled generators and shunt loads.

The effect that transmission line impedance has on conventional impedance relays and the effect it will have on the new pole-slip protection function were evaluated. Transmission line per-unit impedance data was obtained from transmission line manufacturer’s data. This data was processed to obtain a typical per-unit impedance range for transmission lines, which can be used to test the new pole-slip protection function. It was concluded that the effect of the shunt admittance of a transmission line is already included in the transfer angle calculation, since the voltage and current measured at the sending end of the transmission line includes the compensation effect of the shunt admittance. No additional shunt admittances are required to be modelled into the pole-slip protection function, and therefore the transmission line shunt admittance parameters is not required to be known for the new pole-slip function.
The shortcomings of impedance relays, such as network switching configurations and operation with shunt loads were investigated. Recommendations on how to incorporate shunt loads in impedance pole-slip relays were also made. It was suggested to measure the active and reactive power of the transmission line feeders, as well as the active and reactive power of the shunt load feeders. Transmission line feeders were defined as feeders that connect to other power stations via transmission lines. Shunt load feeders were defined as feeders that feed loads like large factories or municipalities and power station internal loads etc. By measuring transmission line feeder currents, it can be determined which transmission lines are in operation. The shunt load feeders were treated as loads that will cause the transfer angle between the generator EMF and the infinite bus to decrease. By measuring the power on the shunt load feeders and the transmission line feeders, the transfer angle can be adjusted accordingly in the new pole-slip protection function.